

Hedge Fund Performance Evaluation under the Stochastic Discount Factor Framework

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Abstract

We study hedge fund performance evaluation under the stochastic discount factor framework of Farnsworth, Ferson, Jackson, and Todd (FFJT). To accommodate dynamic trading strategies and derivatives used by hedge funds, we extend FFJT's approach by considering models with option and time-averaged risk factors and incorporating option returns in model estimation. A wide range of models yield similar conclusions on the performance of simulated long/short equity hedge funds. We apply these models to 2,315 actual long/short equity funds from the Lipper TASS database and find that a small portion of these funds can outperform the market.

I. Introduction

Performance evaluation of actively managed mutual funds and hedge funds is an important issue facing both finance academics and practitioners. Whether some actively managed funds can beat the market has important implications for the efficient market debate. At the same time, identifying funds with superior performance is key to the success of investors who must allocate money among different investment vehicles. Performance evaluation in both theory and practice, however, is challenging because almost all inferences on fund performance depend on the benchmark models used, leading to the well-known joint hypothesis testing problem.

Farnsworth, Ferson, Jackson, and Todd (FFJT) (2002) develop an innovative and effective approach to mutual fund performance evaluation under the stochastic discount factor (SDF) framework. In particular, FFJT examine a wide range of SDF models using both actual and simulated mutual fund returns. By controlling the skill levels of the (hypothetical) manager in delivering abnormal returns, FFJT

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use the simulated fund returns as a benchmark to correct for potential biases of the SDF models in evaluating actual mutual fund returns. As a result, FFJT can better identify the true skill levels of actual managers and find that the average mutual fund has enough abnormal performance to cover transaction costs. Moreover, they show that except for a few models, a wide variety of SDF models used in the literature yield similar conclusions on the true ability of managers based on historical returns, although they tend to have a mild negative bias when true performance is neutral.

Although the FFJT (2002) approach works well for mutual funds, the fast-growing hedge fund industry raises new challenges for performance evaluation because of the investment strategies and compensation structures of hedge funds. Because hedge funds are not subject to the same level of regulation as mutual funds, they enjoy greater flexibility in their investment strategies. As a result, they frequently use short selling, leverage, and derivatives, strategies rarely used by mutual funds, to enhance returns and/or reduce risks. Whereas mutual funds charge a management fee proportional to assets under management, most hedge funds charge an incentive fee, typically 15% to 20% of profits, in addition to a fixed management fee of 1% to 2%. Many funds also have a high-watermark provision, which requires managers to recoup previous losses before receiving incentive fees. The compensation structure might encourage hedge fund managers to use strategies with option-like payoffs to increase upside potential or to protect downside risks of their investments.

It has been widely documented in the literature that hedge funds exhibit option-like returns.¹ For example, Fung and Hsieh (2001) show that the returns of “trend-following” funds are highly nonlinear and resemble the returns of “look-back straddles.” Mitchell and Pulvino (2001) show that the returns of “risk or merger arbitrage” funds have nonlinear exposure to the overall market, with almost zero beta in up markets and big negative beta in down markets. The models used in FFJT (2002) for mutual fund performance evaluation are mostly linear asset pricing models with stock market factors. As such, these models might not be directly applicable to hedge funds because of their derivatives usage and nonlinear returns. For example, Grinblatt and Titman (1989) show that it would be problematic for linear asset pricing models to price nonlinear returns.

In this article, we extend the FFJT (2002) approach to study hedge fund performance evaluation under the SDF framework, which is more suitable than the traditional linear regression approach in dealing with nonlinear hedge fund returns.² To accommodate dynamic trading strategies and derivatives used by hedge funds, we incorporate both options and time-averaged factors into traditional linear asset pricing models, and use option returns in the estimation of the SDF models. Specifically, we consider a wide range of models, which include the

¹TASS, a hedge fund research company, reports that more than 50% of the 4,000 hedge funds it follows use derivatives. Merton (1981), Dybvig and Ross (1985), and others show that dynamic trading strategies could generate option-like returns. For empirical evidence, see, for example, Fung and Hsieh (1997), Agarwal and Naik (2004), and Ben Dor, Jagannathan, and Meier (2003).

²See Cochrane (2005) for a comprehensive treatment of theoretical and empirical asset pricing based on the SDF approach.

unconditional and conditional versions of the capital asset pricing model (CAPM), the Fama–French (1993) model augmented by the momentum factor, the model of Agarwal and Naik (2004) with two option factors, and the 7-factor model of Fung, Hsieh, Naik, and Ramadorai (FHDR) (2008).³ Following Ferson, Henry, and Kisgen (2006) and Patton and Ramadorai (2013), we consider models with time-averaged factors to account for interim trading of hedge funds. We also apply the approach of Getmansky, Lo, and Makarov (2004) to control for potential bias in hedge fund returns due to stale prices and illiquid holdings. The FFJT (2002) approach provides a common platform to systematically study the abilities of these models in identifying the true performance of hedge funds. We estimate all the SDF models using stock and option returns as primitive test assets, ensuring that the estimated models are consistent with derivatives pricing. We find that some of the SDF models can price the 16 primitive test assets reasonably well. In fact, certain SDF models cannot be rejected by the Hansen–Jagannathan (1997) specification test.

We apply the SDF models to the simulated returns of long/short equity hedge funds, whose managers have known abilities in delivering abnormal returns. We focus on long/short equity funds because they represent the largest number of hedge funds and have one of the largest assets under management among all hedge fund strategies in the past two decades. Specifically, we assume that a manager receives signals about the CAPM residuals of the 1,000 largest stocks in the Center for Research in Security Prices (CRSP). The manager would long (short) the stocks with a signal that is better (worse) than the average signal of all stocks. A skilled manager receives signals with higher precision and thus can deliver higher alphas. Applying the SDF models to the simulated hedge fund returns, we find that most models yield similar conclusions on the abnormal performance with reasonable accuracy. Most models have a slight negative bias when the manager has no ability to deliver positive alpha, which is similar to the findings of FFJT (2002) for mutual funds.

Finally, we apply the SDF models to the monthly net-of-fee returns of 2,315 actual long/short equity funds covered by TASS, a comprehensive data set on hedge funds. Simple regression analysis shows that about 58% of the long/short hedge funds have nonlinear exposure to either the market factor or option factors. The simulated hedge fund returns display nonlinearity similar to those observed in the actual hedge fund returns. We compare the distribution of the alphas of the 2,315 actual hedge funds under each SDF model with those of the simulated hedge funds. We find that most hedge funds cannot beat the market, in the sense that their alphas are comparable to those of the simulated funds with low-skilled managers. However, a small portion of these hedge funds do seem to be able to outperform the market, with alphas similar to those of the simulated hedge funds with highly skilled managers. Our results show that the general approach of FFJT (2002) is equally applicable to hedge fund performance evaluation.

³Agarwal and Naik (2004) include option returns as factors in traditional asset pricing models to capture nonlinear hedge fund returns. Fung and Hsieh (2001) propose a 7-factor model, which, in addition to traditional stock, bond, and credit market factors, includes excess returns of portfolios of lookback straddles on currencies, commodities, and bonds.

The remainder of this article is organized as follows: In Section II, we discuss hedge fund performance evaluation under the SDF framework of FFJT (2002). In Section III, we apply a wide range of SDF models to the simulated returns of long/short equity hedge funds with managers of known abilities in delivering abnormal returns. We discuss the data in Section IV and provide empirical evidence on the performance of the 2,315 long/short equity hedge funds in Section V. Section VI concludes the article.

II. Hedge Fund Performance Evaluation under the SDF Framework

In this section, we first introduce the SDF approach of FFJT (2002) for performance evaluation. We then discuss the unique features of hedge fund returns and the SDF models used for hedge fund performance evaluation.

A. The SDF Approach of FFJT

Although the existing literature on mutual fund performance heavily relies on linear asset pricing models, FFJT (2002) is one of the first studies that examines performance evaluation under the general and flexible SDF framework. The fundamental theorem of asset pricing, one of the cornerstones of neoclassical finance, establishes the equivalence between the existence of a positive SDF that correctly prices all primitive test assets and the absence of arbitrage. Suppose we have n primitive test assets with gross returns R_t (an $n \times 1$ vector) at t for $t = 0, 1, \dots, T$. Then for all t , we must have

$$(1) \quad \mathbb{E}[\mathcal{M}_t R_t | \mathcal{F}_{t-1}] = \mathbf{1}_{n \times 1},$$

where $\mathbf{1}_{n \times 1}$ is an $n \times 1$ vector of ones, \mathcal{F}_{t-1} denotes the information set available at time $t - 1$, and $\mathbb{E}[\cdot | \mathcal{F}_{t-1}]$ denotes the conditional expectation given \mathcal{F}_{t-1} . The scalar random variable \mathcal{M}_t discounts total payoffs at t state by state to yield the “present value” at $t - 1$, which is equal to \$1.

For the purpose of performance evaluation, we need to identify a particular SDF, \mathcal{M}_t , which can price all the primitive test assets and thus satisfy equation (1). Then we can use the SDF model to evaluate the performance of actively managed funds. Because it is practically infeasible to include all public information in the empirical estimation of equation (1), the empirical asset pricing literature typically uses predetermined information variables, \mathcal{Z}_{t-1} , which are elements of the public information set \mathcal{F}_{t-1} . By the law of iterated expectations, equation (1) holds when we replace \mathcal{F}_{t-1} with \mathcal{Z}_{t-1} :

$$(2) \quad \mathbb{E}[\mathcal{M}_t R_t | \mathcal{Z}_{t-1}] = \mathbf{1}_{n \times 1}.$$

A conditional approach to performance evaluation allows a researcher to set the standard for what is “superior” information by choosing the public information \mathcal{Z}_{t-1} . When \mathcal{Z}_{t-1} is restricted to be a constant, we have an unconditional measure.

An asset pricing model proposes an SDF, y_t , as a proxy for the true SDF, \mathcal{M}_t . In this article, we define y_t as a function of risk factors and prices of risks:

$$(3) \quad y_t = f(b, \tilde{I}_t),$$

where b is a $k \times 1$ vector of prices of risks, \tilde{f}_t is a $k \times 1$ vector of risk factors, and $f(\cdot)$ is the functional form of y_t . Similar to FFJT (2002), we define the pricing error of a given y_t as:

$$(4) \quad \alpha_t = \mathbb{E}[y_t R_t | \mathcal{Z}_{t-1}] - 1,$$

which measures the difference between the price of R_t implied by y_t and the true SDF, π_t . If y_t prices the primitive assets correctly, then α_t should be 0 for all the primitive assets and their linear combinations.

We estimate the parameters of y_t (i.e., the prices of risks, b) by minimizing the Hansen–Jagannathan (1997) distance (HJ-distance hereafter), which is defined as:

$$\delta = \sqrt{\mathbb{E}(\alpha') \mathbb{E}^{-1}(RR') \mathbb{E}(\alpha)}.$$

The HJ-distance is similar to the generalized method of moments (GMM) objective function when the pricing error, α , is used as the moment condition. Whereas GMM uses the optimal weighting matrix, the HJ-distance uses $\mathbb{E}^{-1}(RR')$ as the weighting matrix. Because $\mathbb{E}^{-1}(RR')$ is the same across different models, it is easier to compare model performance based on the HJ-distance. The HJ-distance also has a nice economic interpretation as the maximum pricing error of all linear payoffs constructed from the primitive assets, R_t , with an unit norm. This makes model comparison based on the HJ-distance economically meaningful. In addition to estimating model parameters (e.g., the risk prices), the HJ-distance also provides a measure of model performance (e.g., the HJ-distance) and a measure of model ability to price primitive assets.

where MKT_t represents the monthly excess return of the market portfolio, proxied by the monthly return of the value-weighted CRSP index in excess of the 1-month risk-free rate. To allow time-varying prices of risks, we consider a conditional version of the CAPM with a conditioning variable, z_{t-1} :

$$(6) \quad y_t^{\text{CAPMIV}} = (b_0 + b_1 z_{t-1}) + (b_2 + b_3 z_{t-1}) \text{MKT}_t.$$

The above two models ignore within-month variations in the risk factors. Next, we consider models with time-averaged factors, using information from daily data. For brevity, we discuss only conditional models with time-averaged factors.⁶ For the conditional CAPM, the pricing model is specified as:

$$(7) \quad y_t^{\text{CAPMIVD}} = b_0 + b_1 z_{D,t-1} + b_2 \text{MKT}_{D,t} + b_3 \text{ZMKT}_{D,t},$$

where $z_{D,t-1}$ is the average of daily observations of the conditioning variable for month $t - 1$, $\text{MKT}_{D,t}$ is the average of daily observations of MKT for month t , and $\text{ZMKT}_{D,t}$ is the average of the product of the daily conditioning variable (from month $t - 1$) and daily MKT for month t . We use the superscript “ D ” to denote models with daily averaged factors.

To capture the cross-sectional patterns in stock returns due to size, value, and momentum effects, we consider the Fama–French (1993) 3-factor model augmented by the momentum factor with the following SDF:

$$(8) \quad y_t^{\text{FF}} = b_0 + b_1 \text{MKT}_t + b_2 \text{SMB}_t + b_3 \text{HML}_t + b_4 \text{MOM}_t,$$

where we incorporate two additional factors from the option market into the CAPM. The first factor, STR_t , is the return on at-the-money (ATM) Standard & Poor's (S&P) 500 index straddles with time to maturity between 20 and 50 days. This factor captures the aggregate volatility risk as in Ang, Hodrick, Xing, and Zhang (2006). The second factor, $SKEW_t$, is the return on out-of-the-money (OTM) S&P 500 index puts that expire in 20 to 50 days. This factor captures jump risk in the market index. The data for option returns are obtained from OptionMetrics. The conditional version of the option-based model is specified as:

$$(12) \quad y_t^{OPTIV} = (b_0 + b_1 z_{t-1}) + (b_2 + b_3 z_{t-1})MKT_t \\ + (b_4 + b_5 z_{t-1})STR_t + (b_6 + b_7 z_{t-1})SKEW_t.$$

The time-averaged version of OPT is specified as:

$$(13) \quad y_t^{OPTIVD} = (b_0 + b_1 z_{D,t-1}) + (b_2 MKT_{D,t} + b_3 ZMKT_{D,t}) \\ + (b_4 STR_{D,t} + b_5 ZSTR_{D,t}) + (b_6 SKEW_{D,t} + b_7 ZSKEW_{D,t}),$$

where $ZSTR_{D,t}$ and $ZSKEW_{D,t}$ are computed in a similar way as $ZMKT_{D,t}$.

The 7-factor model of FHNR (2008) combines option factors with equity factors and has the following SDF:

$$(14) \quad y_t^{FHNR} = b_0 + b_1 MKT_t + b_2 SMB_t + b_3 FXSTR_t \\ + b_4 COSTR_t + b_5 BDSTR_t + b_6 TERM_t + b_7 DEF_t,$$

where the three option factors are constructed from returns of lookback straddles for currencies (FXSTR), commodities (COSTR), and bonds (BDSTR). FHNR also include SMB, TERM (the yield spread between 10-year Treasury bond and 3-month Treasury bill (T-bill)), and DEF (changes in the credit spread between Moody's BAA bond and 10-year Treasury bond) as risk factors. The conditional FHNR model is specified as:

$$(15) \quad y_t^{FHNRIV} = (b_0 + b_1 z_{t-1}) + (b_2 + b_3 z_{t-1})MKT_t + (b_4 + b_5 z_{t-1})SMB_t \\ + (b_6 + b_7 z_{t-1})FXSTR_t + (b_8 + b_9 z_{t-1})COSTR_t \\ + (b_{10} + b_{11} z_{t-1})BDSTR_t + (b_{12} + b_{13} z_{t-1})TERM_t \\ + (b_{14} + b_{15} z_{t-1})DEF_t.$$

We do not consider a time-averaged version of FHNR because we do not have daily returns of the look-back straddles.

Finally, we introduce a new model as an alternative to FHNR (2008) to capture nonlinearities in hedge fund returns. The new model, MIX, mixes the option-based model with the Fama–French (1993) model and has the following SDF:

$$(16) \quad y_t^{MIX} = b_0 + b_1 MKT_t + b_2 SMB_t + b_3 HML_t \\ + b_4 MOM_t + b_5 STR_t + b_6 SKEW_t.$$

The factors of the conditional versions of MIX, MIXIV, and MIXIVD are all scaled by the conditioning variables. Whereas the FHNR model has been developed mainly for trend-following funds, our MIX model might be more appropriate for funds that mainly invest in equities and equity derivatives.

The previous literature has suggested three widely used conditioning variables: 1-month T-bill rate, TERM, and DEF. Because both TERM and DEF have been included as risk factors in the FHN (2008) model, we use the 1-month T-bill rate to scale the risk factors to obtain time-varying market prices of risks. We use TERM and DEF to scale the returns of the primitive test assets to approximate the returns of dynamic trading strategies. We require the SDF models to price both the unscaled and scaled returns of the primitive test assets.

III. Simulated Hedge Fund Returns

To test whether the SDF models can accurately evaluate hedge fund performance, following FFJT (2002), we apply them to simulated hedge fund returns with managers of known abilities in delivering abnormal returns. The simulated hedge fund returns can then serve as a benchmark for evaluating actual hedge fund performance. For example, we can identify the skill levels at which the simulated returns are comparable to the actual returns.

We obtain simulated returns of an artificial long/short equity hedge fund based on the actual returns of the 1,000 largest stocks from CRSP between Jan. 1996 and Dec. 2012, the period for which we have actual hedge fund data. We assume that each month the manager receives a signal about the CAPM residual of each of the 1,000 stocks.⁸ The manager would long (short) the stocks with a signal that is better (worse) than the average signal of all the stocks. A more skilled manager would receive a signal with higher precision and thus can deliver higher abnormal returns on average.

Specifically, we assume that the returns of the 1,000 stocks follow the CAPM relation:

$$(17) \quad r_{it} = \alpha_i + \beta_i r_{mt} + \epsilon_{it},$$

where for each month t , r_{it} is the excess return of stock i , r_{mt} is the excess return of the market portfolio, ϵ_{it} is the idiosyncratic component of the stock return, and α_i and β_i are the intercept and slope coefficients of the CAPM regression, respectively. We assume that at the beginning of each month t , the manager receives a signal, s_{it} , and

$$(18) \quad s_{it} = \gamma \epsilon_{it} + (1 - \gamma) \sigma_i u_{it},$$

where u_{it} represents the noise in the signal and follows an independent and identically distributed standard normal distribution, σ_i measures the full-sample time-series volatility of ϵ_{it} for each firm i , and γ (between 0 and 1) measures the skill level of the manager.⁹ A higher γ means that the manager has a more precise signal about ϵ_{it} . Suppose $\gamma = 1$, then at the beginning of month t , the manager would know whether r_{it} would out- or underperform the market based on his or

⁸We also consider residuals from nonlinear models other than the CAPM and obtain similar results, which are available from the authors.

⁹We also allow the firm-level idiosyncratic volatility to be time varying and estimate σ_i using a 24-month rolling window. We obtain similar results, which are available from the authors.

her signal on ϵ_{it} . The manager then can long or short the stock based on ϵ_{it} and earn abnormal returns.¹⁰

We define $\bar{s}_t = 1/N \sum_{i=1}^N s_{it}$ as the average level of the original signal across the 1,000 stocks at time t , with $N = 1,000$. We assume that the manager longs the stocks with above-average signals and shorts the stocks with below-average signals. Our weights are similar to those used in Khandani and Lo (2011), who also simulate returns on long/short equity hedge funds. To be more specific, for firms with positive signals, the weights are defined as:

$$(19) \quad w_{it}^+ = \frac{(s_{it} - \bar{s}_t) I_{it}^+}{\sum_{i=1}^N (s_{it} - \bar{s}_t) I_{it}^+}, \quad I_{it}^+ = 1 \text{ if } s_{it} > \bar{s}_t, \text{ and } 0 \text{ otherwise.}$$

Similarly, for firms with negative signals, the weights are defined as:

$$(20) \quad w_{it}^- = -\frac{(s_{it} - \bar{s}_t) I_{it}^-}{\sum_{i=1}^N (s_{it} - \bar{s}_t) I_{it}^-}, \quad I_{it}^- = 1 \text{ if } s_{it} < \bar{s}_t, \text{ and } 0 \text{ otherwise.}$$

The portfolio is self-financing, because the weights sum to 0:

$$(21) \quad \sum_{i=1}^N (w_{it}^+ + w_{it}^-) = 1 - 1 = 0.$$

Based on the weights above, the return on the long/short portfolio at t becomes

$$(22) \quad r_p = \sum_{i=1}^N (w_{it}^+ + w_{it}^-) r_{it} = \alpha_{pt} + \beta_{pt} r_{\text{mkt}} + \epsilon_{pt},$$

where $\alpha_{pt} \propto \sum_{i=1}^N (s_{it} - \bar{s}_t) \alpha_i$, $\beta_{pt} \propto \sum_{i=1}^N (s_{it} - \bar{s}_t) \beta_i$, and $\epsilon_{pt} \propto \sum_{i=1}^N (s_{it} - \bar{s}_t) \epsilon_{it}$. We emphasize that the signal is about the idiosyncratic component of the return of each stock. Even though the stock might have a zero α , a manager with a relatively accurate signal can still beat the market, because $E(\epsilon_{pt} | s_t)$ could be nonzero. Moreover, a more accurate signal will lead to higher correlation between portfolio weights and subsequent realized idiosyncratic returns, which will lead to higher excess returns for the portfolio.

Although in theory the long/short portfolio has 0 net investment, in reality one must put down money to initiate both the long and short positions. Meanwhile, a manager with a positive γ can generate positive abnormal returns, which can be further magnified by leverage. The Federal Reserve Board Regulation T allows a maximum leverage ratio of 2:1.¹² About 60% of the 2,315 long/short equity funds in TASS report usage of leverage with an average leverage ratio of about 2:1. In our simulation analysis, we consider two cases: a conservative leverage ratio of 1:1 and a more aggressive leverage ratio of 2:1 as in Khandani and Lo (2011).

IV. The Data

Our empirical analysis mainly relies on monthly observations of the following four types of data between Jan. 1996 and Dec. 2012: i) risk factors for the SDF models, ii) conditioning variables used to capture time-varying prices of risks and/or dynamic trading strategies, iii) returns of primitive test assets used in estimating the SDF models, and iv) returns of 2,315 long/short equity hedge funds from TASS. Table 1 provides the mean, standard deviation, minimum, maximum, and autocorrelation for all the data items used in our analysis.

Panel A of Table 1 provides summary information of the risk factors and the conditioning variables. The first four factors, MKT, SMB, HML, and MOM, are standard stock market factors widely used in the current asset pricing literature and all exhibit positive means and sizable volatilities. The two option factors from Agarwal and Naik (2004), STR and SKEW, capture the volatility and jump risk premiums in the index option market. Consistent with the well-known results in the option pricing literature, the straddle factor earns a negative risk premium. The other three option factors from FHNR (2008), FXSTR, COSTR, and BDSTR, capture the returns of look-back straddles on currencies, commodities, and bonds, respectively. Their summary statistics are very similar to those in FHNR. The three conditioning variables, RF (the 1-month T-bill rate), TERM, and DEF, are all highly persistent and exhibit strong autocorrelations. To account for potential bias in statistical inference due to these persistent conditioning variables, all test statistics on the pricing errors (including the HJ-distance test) are based on Newey–West (1987) adjusted standard errors.¹³

Panel B of Table 1 reports the summary statistics of the primitive test assets used in our estimation of the SDF models. These assets represent the investment opportunity set available to hedge fund managers and have enough return spreads to differentiate candidate SDF models. We first consider 6 stock portfolios sorted by size and book-to-market ratio to capture cross-sectional return differences due to the size and value effects documented in Fama and French (1993). We also consider 6 stock portfolios sorted by size and past returns. The latter represents the

¹²Leverage is defined as the ratio between the total absolute long and short positions and the capital involved in establishing the long and short positions. For example, if the fund has established \$100 long and \$100 short positions with \$100 capital, then the leverage ratio would be 2:1.

¹³Ferson, Sarkissian, and Simin (2008) show that previous studies have overstated the significance of time-varying alphas in models with persistent predictors multiplied by contemporaneous factors. Although we do not have time-varying alphas, we minimize possible biases due to persistent conditioning variables by using Newey–West (1987) adjusted standard errors.

TABLE 1
Summary Statistics

Table 1 provides summary statistics on all the data items used in our empirical analysis. The sample period is between Jan. 1996 and Dec. 2012, which yields 204 months of observations. Panel A reports monthly summary statistics for risk factors and conditioning variables. The first 4 factors, MKT, SMB, HML, and MOM, are standard stock market factors. The 2 option factors, STR and SKEW, capture the volatility and jump risk premiums in the index option market. The other 3 option factors, FXSTR, COSTR, and BDSTR, capture the returns of lookback straddles on currencies, commodities, and bonds, respectively. The 3 conditioning variables are RF (1-month Treasury bill rate), TERM spread (yield difference between 10-year and 3-month Treasury bonds), and DEF spread (yield difference between Baa and Aaa corporate bonds). Panel B includes monthly summary statistics for 15 primitive assets. The first 6 stock portfolios are sorted by size and book-to-market ratio (BM). The second 6 stock portfolios are sorted by size and past returns. The last 3 primitive assets are at-the-money (ATM) calls, ATM puts, and out-of-the-money (OTM) puts on the S&P 500 index. Panel C reports monthly summary statistics of 2,315 long/short equity hedge funds from TASS. Panel D reports nonlinearities in hedge fund returns. The 2,315 hedge fund returns are regressed on 2 sets of factors. The first regression includes MKT, MKT², and MKT³, whereas the second includes MKT, STR, and SKEW. We report the mean, standard deviation, and percentage of the regression coefficients that are statistically significant.

<u>Factors</u>	<u>Mean</u>	<u>Std Dev</u>	<u>Minimum</u>	<u>Maximum</u>	<u>Rho</u>
<i>Panel A. Summary Statistics of the Risk Factors and Conditioning Variables</i>					
MKT	0.0047	0.0476	-0.1723	0.1134	0.1173
SMB	0.0025	0.0366	-0.1639	0.2200	-0.0794
HML	0.0028	0.0348	-0.1260	0.1384	0.1160
MOM	0.0043	0.0570	-0.3474	0.1839	0.0750
STR	-0.3254	0.7252	-1.3384	2.9177	-0.0339
SKEW	-0.3664	0.8804	-0.9792	5.1544	0.1222
FXSTR	-0.0193	0.1511	-0.2663	0.6886	0.1109
COSTR	-0.0034	0.1857	-0.3000	0.6922	0.0365
BDSTR	-0.0001	0.1396	-0.2465	0.6475	-0.0287
RF	0.0023	0.0018	0.0000	0.0056	0.9791
TERM	0.0199	0.0137	-0.0023	0.0415	0.9886
DEF	0.0102	0.0047	0.0055	0.0338	0.9623
<u>Assets</u>	<u>Mean</u>	<u>Std Dev</u>	<u>Minimum</u>	<u>Maximum</u>	<u>Rho</u>
<i>Panel B. Summary Statistics of the Returns of the Primitive Test Assets</i>					
Small low BM	0.0066	0.0747	-0.2436	0.2816	0.0898
Small med BM	0.0111	0.0564	-0.1928	0.1668	0.1286
Small high BM	0.0121	0.0593	-0.2030	0.1806	0.1981
Big low BM	0.0073	0.0471	-0.1505	0.1018	0.0715
Big med BM	0.0077	0.0477	-0.1731	0.1260	0.1485
Big high BM	0.0073	0.0522	-0.2254	0.1627	0.1726
Small low MOM	0.0080	0.0868	-0.2566	0.4632	0.1905
Small med MOM	0.0104	0.0539	-0.2073	0.2202	0.1736
Small high MOM	0.2073	622202			

winner and loser portfolios and thus captures the momentum effect of Jegadeesh and Titman (1993). The 12 stock portfolios cover the most popular investment styles for equity investors. Next, we include returns of ATM calls, ATM puts, and OTM puts on the S&P 500 index, which are among the most widely traded options in the world. Finally, we include the 1-month risk-free rate to anchor the mean of the SDF models. Panel B reports the summary statistics of the first 15 test assets, whereas the 1-month risk-free rate is summarized in Panel A of Table 1. Consistent with the existing literature, we find that value firms have higher returns than growth firms and winner firms have higher returns than loser firms. Compared to stock returns, option returns have much higher means and volatilities.

The hedge fund data used in our analysis are obtained from TASS, which is probably the most comprehensive data set used in the current hedge fund literature. The data set covers more than 4,000 funds from Nov. 1977 to Dec. 2012, which are classified into “live” and “graveyard” funds. The graveyard database did not exist before 1994. To mitigate the problem of survivorship bias, we consider both live and graveyard funds and restrict our sample to the period between Jan. 1996 and Dec. 2012. The database provides monthly net-of-fee returns and net asset values for each fund.

The hedge funds covered by TASS follow 11 investment styles and trade in a wide range of markets. Therefore, it is difficult to replicate the trading strategies and derivatives used by every hedge fund strategy. We focus on long/short equity hedge funds because they cover the largest number of hedge funds in TASS and have one of the largest group of assets under management during our sample period.¹⁴ Specifically, we have 2,315 long/short equity hedge funds in TASS.

Panel C of Table 1 reports the distribution of the summary statistics for 4 quartiles of the net-of-fee monthly returns of the 2,315 hedge funds. We see that the mean monthly returns range from -0.01% in the lowest quartile to 1.69% in the highest quartile, and the standard deviation increases from 5.26% to 7.67% . Panel D highlights the exposure of hedge fund returns to nonlinear market factors and option factors. We consider two regressions of individual hedge fund returns. In the first regression, the independent variables include the market factor and its second and third moments. In the second regression, we include the market, straddle, and skewness factors. In both regressions, we find that about 60% to 70% of hedge funds have significantly nonzero loadings on the market factor, which means that these funds are not exactly market neutral. About 16% (26%) of the hedge funds have significant nonzero exposures to the second (third) moment of the market factor. About 26% (29%) of the hedge funds have significant nonzero exposures to the straddle (skewness) factors. Collectively, about 58% of the long/short hedge funds have significant exposures to at least one of the nonlinear factors constructed on the market portfolio.¹⁵

One common interpretation of nonlinearity in fund returns is that it reflects market-timing ability of managers. Treynor and Mazuy (1966) provide the classical connection between market timing and nonlinearity. Chen, Ferson, and

¹⁴The total asset under management in the long/short category reported in TASS is about \$170 billion as of 2012.

¹⁵This number can not be deduced directly from Panel D of Table 1 because many stocks have significant exposures to multiple nonlinear factors.

Peters (2010) consider the issue of identifying true market-timing ability and examine different categories of biases that lead to nonlinearity. After controlling for these biases, the authors find positive evidence of market-timing ability for bond fund managers. A more recent paper by Cao, Chen, Liang, and Lo (2013) shows that hedge fund managers can even time market liquidity. In fact, FFJT (2002) consider a separate simulation design just to mimic the market-timing ability of mutual fund managers. The nonlinearity we observe in hedge fund returns could be due to market timing by hedge fund managers or nonlinear exposures of the stocks held by the funds. In results not reported here, we find that the returns of roughly 30% of the 1,000 stocks in our sample have significant loadings on the nonlinear factors. This suggests that the nonlinearity in hedge fund returns could be driven by the nonlinearity in the returns of the stocks they hold. Although we do not rule out the possibility that hedge fund managers could time the market, in our simulation and empirical analysis, we focus on stock picking, which is likely the most important source of alpha and one of the main appeals of long/short equity hedge funds.

V. Empirical Results on Hedge Fund Performance Evaluation

In this section, we provide empirical analysis of the performance of the 2,315 long/short equity hedge funds using the SDF approach. First, we estimate all the SDF models using the 16 primitive test assets and identify models that can price the test assets well. Second, we apply the SDF models to evaluate simulated hedge fund returns to gauge their power to detect abnormal performance when the ability of the manager is known. Finally, we apply the SDF models to evaluate the returns of the 2,315 long/short equity hedge funds, using the results for the simulated returns as a benchmark to adjust for potential biases in the SDF models.

A. Estimating the SDF Models

Table 2 reports the empirical results on the estimation of the SDF models. Panel A contains the results based on the returns of the 16 primitive test assets. Panels B and C contain the results based on the returns of the primitive assets scaled by TERM and DEF, respectively. In each panel, we report the estimated HJ-distance, the asymptotic p -values of the specification test based on the HJ-distance, as well as p -values based on the finite-sample empirical distribution of the HJ-distance to correct for potential biases in the asymptotic distribution.¹⁶ We also report the mean, standard deviation, minimum, and maximum of each

¹⁶Previous studies (e.g., Ferson and Foerster (1994)) show that asymptotic tests based on 2-stage GMM estimation tend to overreject the null hypothesis. Ahn and Gadarowski (2004) find similar overrejection problem for the HJ-distance estimation. To correct the overrejection bias, our empirical p -values are estimated from 5,000 simulations. For each simulation, we first generate returns by using model-implied expected returns with normally distributed noises. That is, from the pricing equation $E(yr) = p$, under the null, $E(r) = [p - \text{cov}(y, r)]/E(y)$. Next, we estimate the HJ-distance for each simulated sample of returns. The empirical p -values are calculated as percentages of HJ-distances estimated over simulations that are bigger than the HJ-distance estimated from real data.

TABLE 2
 Estimation of the SDF Models Based on the 16 Primitive Test Assets

Table 2 reports the empirical results of the estimation of the stochastic discount factor (SDF) models. Our sample period is from Jan. 1996 to Dec. 2012, with 204 monthly observations. Panel A contains the results based on the returns of the 16 primitive test assets. Panels B and C contain the results based on the scaled returns of the primitive assets by term premium (TERM) and default premium (DEF), respectively. In each panel, we report the estimated Hansen–Jagannathan (1997) distance (HJ-Dist) of each model, as well as the mean, standard deviation, minimum, and maximum of each estimated SDF model. We report the asymptotic and empirical p -values of the specification test based on the HJ-distance for all the SDF models.

SDF Models	HJ-Dist d	$p(d = 0)$	Empirical $p(d = 0)$	Mean	Std Dev	Min	Max
<i>Panel A. Estimation of the SDF Models Based on the Returns of the Primitive Assets</i>							
CAPM	0.985	0%	0%	0.998	0.103	0.762	1.380
CAPMIV	0.978	0%	0%	0.998	0.210	0.452	1.963
CAPMIVD	0.969	0%	0%	0.998	0.305	0.241	2.429
FF	0.967	0%	0%	0.998	0.216	0.437	1.863
FFIV	0.780	2%	0%	0.997	2.039	-4.052	9.788
FFIVD	0.681	21%	8%	0.998	2.643	-6.284	12.159
OPT	0.773	0%	6%	0.998	0.623	-0.597	5.172
OPTIV	0.699	19%	12%	0.999	1.762	-4.268	10.498
OPTIVD	0.525	6%	86%	0.998	1.701	-13.687	9.439
FHNR	0.805	1%	0%	0.998	1.357	-2.050	5.659
FHNRIV	0.000			0.980	23.537	-56.808	99.977
MIX	0.733	0%	6%	0.998	0.671	-0.889	5.465
MIXIV	0.351	45%	37%	0.998	4.026	-11.893	17.997
MIXIVD	0.185	68%	82%	1.000	2.837	-17.176	10.854
<i>Panel B. Estimation of the SDF Models Based on the Returns of the Primitive Assets Scaled by TERM</i>							
CAPM	0.913	0%	0%	0.997	0.125	0.713	1.459
CAPMIV	0.339	6%	100%	0.995	1.469	-1.224	4.311
CAPMIVD	0.339	5%	100%	0.995	1.466	-1.201	4.238
FF	0.896	0%	0%	0.997	0.268	-0.564	1.994
FFIV	0.192	61%	100%	0.995	2.124	-5.334	12.112
FFIVD	0.185	79%	100%	0.995	2.227	-5.778	10.088
OPT	0.832	0%	1%	0.997	0.529	-0.212	4.690
OPTIV	0.315	3%	100%	0.995	1.599	-2.208	4.886
OPTIVD	0.259	23%	100%	0.995	1.773	-1.540	7.949
FHNR	0.693	0%	57%	0.996	1.509	-4.195	5.292
FHNRIV	0.000	89%		0.995	2.702	-6.201	6.880
MIX	0.804	0%	1%	0.997	0.602	-0.821	5.228
MIXIV	0.104	66%	95%	0.995	2.625	-8.788	10.553
MIXIVD	0.102	79%	95%	0.995	2.747	-8.261	13.394
<i>Panel C. Estimation of the SDF Models Based on the Returns of the Primitive Assets Scaled by DEF</i>							
CAPM	1.001	0%	0%	0.997	0.071	0.836	1.260
CAPMIV	0.831	0%	5%	0.995	1.606	-1.285	3.621
CAPMIVD	0.832	0%	2%	0.995	1.583	-1.125	4.016
FF	0.986	0%	0%	0.997	0.199	0.409	1.781
FFIV	0.511	31%	52%	0.994	2.854	-5.656	10.991
FFIVD	0.473	42%	62%	0.994	2.854	-6.029	12.924
OPT	0.838	0%	0%	0.997	0.611	-0.570	5.010
OPTIV	0.701	0%	8%	0.995	1.717	-3.061	4.633
OPTIVD	0.547	1%	60%	0.997	1.788	-13.650	10.053
FHNR	0.774	0%	5%	0.997	1.389	-2.248	6.120
FHNRIV	0.000	46%		0.993	6.306	-13.452	20.826
MIX	0.807	0%	0%	0.997	0.652	-0.965	5.321
MIXIV	0.404	9%	22%	0.995	3.000	-8.430	13.742
MIXIVD	0.223	58%	67%	0.997	3.619	-12.920	12.483

estimated SDF model, \hat{y}_t . Because the results in Panels B and C based on the scaled returns of the primitive assets are similar to those in Panel A, we focus our discussion on the results in Panel A.¹⁷

¹⁷We also consider exponential models in addition to linear models. The advantage of exponential models is that they will always be nonnegative and thus do not allow arbitrage opportunities.

Among the unconditional models, the CAPM has the highest HJ-distance (0.985), followed by FF (0.967), FHN (0.805), OPT (0.773), and MIX (0.733). The fact that MIX has smaller HJ-distance than FHN highlights the importance of the three stock market factors (SMB, HML, and MOM) and the two option factors (STR and SKEW) for pricing the primitive test assets. All the conditional models using monthly information (CAPMIV, FFIV, OPTIV, FHNIV, and MIXIV) have much smaller HJ-distances than their unconditional counterparts. FHNIV has a 0 HJ-distance, because with 16 parameters it can fit 16 assets perfectly. The models with time-averaged factors (CAPMIVD, FFIVD, OPTIVD, and MIXIVD) have even smaller HJ-distances than the models with monthly factors, highlighting the importance of considering interim trading and within-month variations.

All the unconditional models except FHN (2008) are overwhelmingly rejected by the specification test based on the HJ-distance with 0 asymptotic p -values. Using the empirical p -values based on finite-sample simulations, which are generally larger than asymptotic p -values, we cannot reject the null hypothesis that OPT and MIX are correctly specified at the 5% confidence level (the empirical p -values are 6%). The asymptotic p -values of the specification test based on the HJ-distance for the four conditional models with monthly information, CAPMIV, FFIV, OPTIV, and MIXIV, are 0%, 2%, 19%, and 45%, respectively. The p -values of the conditional models with time-averaged factors are mostly higher than those with monthly factors. However, it should be noted that the conditional models tend to be more volatile, and their estimated SDF models are more likely to take extreme values, especially for those with time-averaged factors. To summarize, we cannot reject the null hypothesis that certain models, such as FFIV, FFIVD, OPTIV, OPTIVD, FHNIV, MIX, MIXIV, and MIXIVD, can price the primitive assets.

Table 3 reports time-series averages of the monthly pricing errors (alphas), as defined in equation (4), of the 16 test assets under all the SDF models. The results for the unconditional and corresponding conditional models are displayed next to each other for ease of comparison. The risk-free rate helps anchor the mean of the SDF models, and as a result, most models can price the risk-free rate well. CAPM, CAPMIV, and CAPMIVD, which do not include the SMB and HML factors, tend to have big pricing errors for the size and book-to-market portfolios. In contrast, by including the SMB and HML factors, FF, FFIV, and FFIVD have much smaller pricing errors for the size and book-to-market portfolios. Most models without option factors have relatively large pricing errors for the ATM calls, ATM puts, and OTM puts. For example, the pricing errors of the three options range from about -9% to -30% for CAPM and FF type of models. Although FHN (2008) includes option straddle factors, it still has relatively large pricing errors for the three options, with pricing errors ranging from about 5% to 18%. By including the STR and SKEW factors, OPT, OPTIV, and OPTIVD reduce the pricing errors of the three options to about 6% to 7%. Finally, MIX, MIXIV, and MIXIVD have small pricing errors for both the 12 stock portfolios and the option returns,

However, the exponential models do not perform better than the linear models we considered, and we do not report them in this article.

TABLE 3
Pricing Errors of Primitive Test Assets under the SDF Models

Table 3 reports the time-series average of the monthly pricing errors defined in equation (4) of the 16 primitive test assets under all the stochastic discount factor (SDF) models. Our sample period is from Jan. 1996 to Dec. 2012, with 204 monthly observations. The results for the unconditional and corresponding conditional models are displayed next to each other for ease of comparison.

Test Assets	CAPM	CAPMIV	CAPMIVD	FF	FFIV	FFIVD	OPT	OPTIV	OPTIVD	FHNR	MIX	MIXIV	MIXIVD
RF	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%
Small low BM	-0.22%	-0.26%	-0.31%	-0.27%	-0.35%	-0.35%	0.01%	0.24%	0.23%	-0.21%	-0.23%	-0.22%	-0.07%
Small med BM	0.39%	0.55%	0.63%	0.09%	0.10%	0.09%	0.63%	0.51%	0.39%	-0.26%	0.10%	-0.04%	-0.02%
Small high BM	0.47%	0.73%	0.86%	0.05%	0.03%	0.03%	0.72%	0.65%	0.55%	-0.17%	0.03%	0.08%	0.03%
Big low BM	0.01%	-0.06%	-0.10%	0.12%	0.23%	0.21%	-0.04%	-0.03%	-0.02%	0.20%	0.14%	0.10%	0.03%
Big med BM	0.09%	0.22%	0.30%	-0.05%	-0.29%	-0.26%	0.06%	-0.11%	-0.29%	-0.33%	-0.12%	-0.08%	-0.02%
Big high BM	0.04%	0.31%	0.46%	-0.20%	-0.16%	-0.18%	0.19%	-0.06%	-0.14%	-0.50%	-0.12%	-0.20%	-0.07%
Small low MOM	-0.18%	0.03%	0.12%	0.03%	-0.18%	-0.24%	0.14%	-0.48%	0.16%	-0.45%	0.07%	-0.17%	0.09%
Small med MOM	0.34%	0.53%	0.63%	0.11%	0.17%	0.09%	0.49%	0.16%	0.28%	-0.25%	0.06%	-0.13%	-0.05%
Small high MOM	0.50%	0.49%	0.48%	0.12%	0.07%	0.04%	0.76%	0.96%	0.92%	0.47%	0.19%	-0.18%	-0.02%
Big low MOM	-0.34%	-0.19%	-0.12%	0.03%	0.10%	0.09%	-0.24%	-1.09%	-0.55%	-0.92%	0.09%	-0.05%	-0.16%
Big med MOM	0.03%	0.12%	0.17%	0.04%	0.04%	0.11%	-0.08%	-0.31%	-0.28%	-0.19%	-0.07%	-0.19%	-0.01%
Big high MOM	0.18%	0.12%	0.11%	-0.06%	-0.15%	-0.19%	0.19%	0.48%	0.48%	0.36%	-0.03%	-0.04%	-0.06%
ATM call	-14.93%	-15.68%	-15.33%	-14.49%	-16.76%	-14.26%	-6.88%	-6.23%	-1.20%	-4.78%	-6.52%	-1.45%	0.08%
ATM put	-16.91%	-15.49%	-14.19%	-17.58%	-8.57%	-4.46%	6.87%	6.24%	1.20%	-11.41%	6.52%	1.45%	-0.08%
OTM put	-29.25%	-27.50%	-25.82%	-29.84%	-14.89%	-8.93%	0.00%	0.00%	0.00%	-18.68%	0.00%	0.00%	0.00%

highlighting the importance of including both stock and option factors for pricing the 16 test assets.¹⁸

In summary, the results in Tables 2 and 3 show that certain SDF models (e.g., MIX and most conditional models) can price the 16 primitive test assets reasonably well. The conditional models can be further improved by using time-averaged factors instead of monthly factors. In fact, these SDF models cannot be rejected by the specification test based on the HJ-distance. Because no model is perfect, the key in performance evaluation is to adjust the potential biases of the SDF models in actual applications. The SDF framework of FFJT (2002) provides a common platform on which we can examine this issue and make appropriate adjustments.

B. Evaluating Simulated Hedge Fund Returns

Before applying the above SDF models to evaluate actual hedge fund returns, we first examine their ability to identify abnormal performance in a controlled experiment where the manager's ability to deliver superior return is known. Based on the simulation procedure described in Section II, we generate monthly returns of a simulated long/short equity fund at different levels of γ , which reflects different levels of the manager's ability to forecast future idiosyncratic returns. Following FFJT (2002), we evaluate the performance of the artificial hedge fund by estimating the SDF models using the returns of the fund and the 16 primitive assets.

The simulation procedure in Section II does not take fees into account. Given that the actual hedge fund returns are net of fee, our simulations consider both before- and after-fee returns by incorporating management and incentive fees, as well as a standard high-watermark provision.¹⁹ The management and incentive fees for most funds are slightly lower than 2% and 20%, respectively. We adopt an aggressive fee structure with a 2% annual management fee and 20% incentive fee to obtain the simulated after-fee returns.²⁰

Table 4 provides summary information on simulated hedge fund returns. Specifically, it reports the mean, standard deviation, minimum, maximum, market beta, and Sharpe ratio of the monthly returns of the simulated hedge funds at different skill levels. We report before- and after-fee returns based on scaled and unscaled signals at different leverage ratios.

¹⁸

TABLE 4
 Simulated Long/Short Hedge Fund Returns

Table 4 reports the mean, standard deviation, minimum, maximum, market beta, and Sharpe ratio of the monthly before- and after-fee returns of the artificially generated long/short hedge funds at different skill levels based on two related signals. The first signal is about the CAPM residual of the 1,000 largest stocks in Center for Research in Security Prices (CRSP) (each month from Jan. 1996 to Dec. 2012), whereas the second signal is the first signal scaled by its variance. The manager would long (short) the stocks with a signal that is better (worse) than the average signal of all the stocks. A more skilled manager with higher γ would receive a more precise signal and can generate higher alphas on average. We consider a 2% management fee, 20% incentive fee, and the standard high-watermark provision.

<u>Skill γ</u>	<u>Mean</u>	<u>Std Dev</u>	<u>Min</u>	<u>Max</u>	<u>MKT Beta</u>	<u>Sharpe Ratio</u>
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Panel A. Simulated Before-Fee Hedge Fund Returns with Original Unscaled Signal, Leverage 1:1

positive returns. The betas of the artificial hedge fund returns are not exactly 0 but are generally low. The returns in Panel B based on the scaled signal have lower mean, lower standard deviation, and less dispersion, but higher Sharpe ratio than those in Panel A, because less money would be put into stocks with more volatile idiosyncratic risk. The higher Sharpe ratio is consistent with the idea that the scaled signal reflects a better trade-off between risk and return than the unscaled signal. The betas of the simulated returns based on the scaled signal are also closer to 0.

The after-fee returns based on the scaled signal at the 1:1 leverage ratio reported in Panel C of Table 4 are obviously lower than the before-fee returns and more significantly so for higher manager skill levels. For instance, for $\gamma = 0.2$, the average monthly after-fee return is 1.80%, which is 61 bps lower than the average before-fee return in Panel B. For $\gamma = 0.9$, however, the average monthly after-fee return based on the scaled signal becomes 8.12%, which is 2.28% less than the before-fee return in Panel B. This indicates that when the manager skill level increases, managers deliver more abnormal returns and at the same time earn more fees.

Panel D of Table 4 reports the after-fee returns based on the scaled signal with a 2:1 leverage ratio. Intuitively, when the leverage ratio is high, managers are more willing to take risk and the fund returns are higher, with higher volatilities. For the higher leverage ratio of 2:1, when γ increase from 0.1 to 0.9, the average fund returns increase from 1.81% to 17.46%; for the lower leverage ratio of 1:1, the corresponding numbers are 0.75% and 8.12%.

Our ultimate goal is to use the simulated returns as a benchmark to evaluate actual hedge fund returns. Therefore, for the rest of the article, we mainly focus on after-fee returns based on the scaled signal at different leverage ratios to better re-

TABLE 5
Abnormal Returns of Simulated Long/Short Equity Hedge Funds under 10 SDF Models

Table 5 reports the monthly abnormal returns (alphas) of the before- and after-fee returns of simulated long/short equity hedge funds under 10 stochastic discount factor (SDF) models for different levels of manager skill (γ). The alphas are calculated as the time-series averages of the pricing errors defined in equation (4) under each SDF model. Based on the Newey–West (1987) adjusted standard deviation of the time series of the pricing errors for each model, we calculate whether the alphas are significantly different from 0. *, **, and *** indicate significance at the 10%, 5%, and 1% levels, respectively. The signal is scaled by its variance.

SDF Models	Skill γ										
	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
<i>Panel A. Abnormal Returns of the After-Fee Returns of Simulated Long/Short Equity Hedge Funds, Leverage 1:1</i>											
CAPM	-0.33%***	0.61%***	1.69%***	2.92%***	4.21%***	5.49%***	6.63%***	7.53%***	8.14%***	8.45%***	8.54%***
CAPMIV	-0.10%*	0.61%***	1.15%	1.64%	2.18%	2.73%	3.27%	3.75%	4.12%	4.32%	4.39%
CAPMIVD	-0.10%*	0.61%***	1.15%	1.64%	2.17%	2.73%	3.26%	3.74%	4.11%	4.31%	4.38%
FF	-0.33%***	0.61%***	1.71%***	2.95%***	4.26%***	5.54%***	6.68%***	7.58%***	8.18%***	8.49%***	8.58%***
FFIV	-0.09%	0.49%*	0.71%	0.94%	1.20%	1.47%	1.74%	1.97%	2.16%	2.26%	2.30%
FFIVD	-0.08%	0.34%	0.53%	0.75%	0.99%	1.23%	1.46%	1.65%	1.79%	1.87%	1.89%
OPT	-0.30%***	0.71%***	1.89%***	3.20%***	4.58%***	5.90%***	7.06%***	7.95%***	8.54%***	8.84%***	8.93%***
OPTIV	-0.02%	0.71%***	0.78%	0.89%	1.05%	1.24%	1.44%	1.65%	1.84%	1.97%	2.02%
OPTIVD	-0.03%	0.55%***	1.05%	1.52%	2.03%	2.56%	3.06%	3.49%	3.81%	3.97%	4.02%
FHNR	-0.23%**	0.19%	0.61%	1.15%	1.76%	2.38%	2.96%	3.41%	3.72%	3.88%	3.93%
FHNRIV	-0.01%	-0.01%	-0.02%	-0.03%	-0.03%	-0.04%	-0.04%	-0.04%	-0.04%	-0.04%	-0.04%
MIX	-0.30%***	0.72%***	1.90%***	3.23%***	4.61%***	5.94%***	7.10%***	7.98%***	8.57%***	8.86%***	8.95%***
MIXIV	-0.02%	0.44%	0.50%	0.62%	0.78%	0.95%	1.13%	1.28%	1.38%	1.42%	1.44%
MIXIVD	0.00%	0.13%	0.28%	0.36%	0.47%	0.58%	0.69%	0.79%	0.87%	0.91%	0.92%
Average across models	-0.14%	0.48%	1.00%	1.56%	2.16%	2.76%	3.32%	3.77%	4.09%	4.25%	4.30%
<i>Panel B. Abnormal Returns of the After-Fee Returns of Simulated Long/Short Equity Hedge Funds, Leverage 2:1</i>											
CAPM	-0.34%***	1.51%***	3.68%***	6.13%***	8.73%***	11.28%***	13.56%***	15.36%***	16.58%***	17.21%***	17.38%***
CAPMIV	-0.20%***	1.14%***	1.96%	2.92%	3.95%	5.00%	6.00%	6.87%	7.53%	7.88%	8.00%
CAPMIVD	-0.19%***	1.14%***	1.95%	2.91%	3.94%	4.99%	5.98%	6.85%	7.51%	7.86%	7.98%
FF	-0.36%***	1.52%***	3.72%***	6.20%***	8.81%***	11.37%***	13.66%***	15.46%***	16.66%***	17.29%***	17.46%***
FFIV	-0.21%	1.10%	1.77%	2.62%	3.59%	4.62%	5.62%	6.39%	7.02%	7.39%	7.53%
FFIVD	-0.20%	0.52%	0.85%	1.30%	1.77%	2.23%	2.65%	2.98%	3.22%	3.35%	3.39%
OPT	-0.28%***	1.73%***	4.08%***	6.71%***	9.46%***	12.10%***	14.41%***	16.20%***	17.38%***	17.99%***	18.16%***
OPTIV	-0.01%	1.01%	1.09%	1.41%	1.76%	2.12%	2.48%	2.84%	3.15%	3.36%	3.45%
OPTIVD	-0.08%	1.01%	1.78%	2.68%	3.66%	4.65%	5.56%	6.33%	6.89%	7.17%	7.25%
FHNR	-0.30%**	0.53%	1.43%	2.55%	3.81%	5.12%	6.32%	7.28%	7.93%	8.29%	8.40%
FHNRIV	-0.02%	-0.02%	-0.04%	-0.06%	-0.07%	-0.08%	-0.08%	-0.09%	-0.09%	-0.09%	-0.09%
MIX	-0.30%***	1.73%***	4.10%***	6.76%***	9.52%***	12.18%***	14.49%***	16.27%***	17.43%***	18.03%***	18.20%***
MIXIV	0.02%	0.52%	0.70%	0.99%	1.31%	1.64%	1.96%	2.22%	2.39%	2.46%	2.49%
MIXIVD	0.00%	0.25%	0.38%	0.57%	0.78%	0.99%	1.18%	1.34%	1.47%	1.52%	1.54%
Average across models	-0.18%	0.95%	1.91%	3.05%	4.25%	5.44%	6.52%	7.39%	7.99%	8.31%	8.40%

the market. When $\gamma \geq 0.1$, we find positive alphas that increase with γ under most SDF models. Interestingly, most models lead to similar inferences regarding the abnormal performance of the simulated hedge funds. The alphas under most of the unconditional models share similar magnitudes for a given γ . For instance, when γ increases from 0.1 to 0.9, the after-fee monthly alphas for most unconditional models increase from less than 1% to around 8.5%. The conditional models with either monthly information or time-averaged factors have a similar pattern, but on average have smaller alphas than the unconditional models, especially for SDFs with time-averaged factors. When γ increases from 0.1 to 0.9, the after-fee monthly alphas for the conditional models increase from less than 1% to around 2% to 4%. This suggests that part of the alphas under the unconditional models may be attributable to time-varying market prices of risks or interim trading. There is a concern that the conditional models might have too many factors, which tend to overfit the data and lead to smaller but more volatile pricing errors. For instance, though most alphas are small and not statistically significant under FHNRIV, the model could have overfitted the data and failed to detect true skills. Based on results presented in Panel B, we reach similar conclusions about the performance of hedge funds with a 2:1 leverage ratio, though this higher leverage ratio leads to higher alphas.

Overall, the results in Tables 4 and 5 show that most of the SDF models deliver similar evaluation results: They are able to detect the abnormal performance of the simulated hedge fund returns, though most models exhibit a slight negative bias when the managers have no skill. Therefore, at least in situations that are not too different from our simulation setup, the SDF approach of FFJT (2002) is an effective methodology for evaluating hedge fund performance (after correcting for the negative bias).

C. Evaluating Actual Hedge Fund Performance

In this section, we apply the SDF models to evaluate the performances of 2,315 long/short equity hedge funds. Following FFJT (2002), we evaluate the performance of an actual hedge fund by estimating the SDF models using the returns of the hedge fund and the 16 primitive test assets.

TASS directly reports after-fee hedge fund returns. However, there is a concern that because of illiquid assets held by some hedge funds, stale prices may cause the observed raw returns of the hedge funds to be biased. To correct for the potential bias caused by stale prices in hedge fund returns, Getmansky et al. (2004) fit econometric models (e.g., autoregressive moving average (ARMA) models) to hedge fund returns to remove autocorrelations induced by stale prices. The residuals plus the intercepts from the fitted model are then used as “actual” hedge fund returns for performance evaluation. In our situation, long/short equity funds are more likely to use equity and equity derivatives, which are relatively easy to trade. As a result, the bias for long/short equity funds might be less severe than that for funds that hold illiquid assets (e.g., real estate). Still, to be conservative, following Getmansky et al., we fit an ARMA(1, 1) model to the actual hedge fund returns and then use the residuals as “actual” hedge fund returns to rank their performance.

Table 6 provides summary information for the monthly abnormal returns of the 2,315 hedge funds. Panel A contains results based on raw hedge fund returns, and Panel B reports results based on fund returns adjusted for stale price bias. Specifically, we calculate the alphas under each SDF model for all funds and report the alphas of the funds ranked at different percentiles of the entire group. In general, removing autocorrelation in hedge fund returns lowers fund alphas, and we focus our discussion on the adjusted returns in Panel B. The average monthly alphas for all the SDF models are -3.37% (2.24%) for the bottom (top) 1 percentile of all 2,315 hedge funds. Panel A of Table 5 shows that the average after-fee alpha for simulated returns across different models is -0.14% when $\gamma = 0$. This indicates that the lowest 1% of the actual long/short equity funds clearly underperform the market. In fact, the median alpha of the 2,315 actual hedge funds, averaged across models, is -0.25% , which means that the bottom 50% of the hedge fund managers do not display significant skills in outperforming the market when benchmarked against the simulated returns. The alphas of the top 10% (90th percentile) and 1% (99th percentile) of the actual funds, averaged across

TABLE 6
Abnormal Returns of Actual Long/Short Equity Hedge Funds under 10 SDF Models

Table 6 provides the monthly summary information of the abnormal returns (alphas) of the 2,315 hedge funds from TASS. Our sample contains monthly observations from Jan. 1996 to Dec. 2012. Specifically, we calculate the alpha under each stochastic discount factor (SDF) model for all the funds and report the alphas of the funds ranked at the bottom and top 1%, 2.5%, 5%, 10%, 25%, and 50% of the entire group.

SDF Models	1%	2.50%	5%	10%	25%	50%	75%	90%	95%	97.50%	99%
<i>Panel A. Using Raw Hedge Fund Return Data</i>											
CAPM	-1.85%	-1.02%	-0.67%	-0.36%	0.03%	0.37%	0.73%	1.21%	1.70%	2.13%	3.09%
CAPMIV	-3.58%	-1.94%	-1.17%	-0.63%	-0.07%	0.31%	0.70%	1.25%	1.74%	2.55%	3.92%
CAPMIVD	-3.62%	-1.95%	-1.31%	-0.65%	-0.09%	0.31%	0.71%	1.27%	1.77%	2.64%	4.09%
FF	-1.71%	-1.09%	-0.71%	-0.43%	-0.04%	0.31%	0.66%	1.12%	1.60%	2.08%	2.79%
FFIV	-3.93%	-2.31%	-1.69%	-0.99%	-0.28%	0.19%	0.68%	1.33%	2.00%	2.81%	3.89%
FFIVD	-3.82%	-2.17%	-1.41%	-0.95%	-0.33%	0.17%	0.66%	1.37%	2.05%	2.90%	4.26%
OPT	-2.60%	-1.60%	-1.14%	-0.66%	-0.11%	0.34%	0.83%	1.55%	2.23%	2.76%	3.63%
OPTIV	-3.36%	-2.10%	-1.45%	-0.80%	-0.22%	0.23%	0.71%	1.42%	2.18%	2.95%	4.54%
OPTIVD	-3.63%	-2.12%	-1.35%	-0.86%	-0.30%	0.19%	0.72%	1.47%	2.13%	3.20%	4.54%
FHNR	-3.42%	-2.05%	-1.55%	-0.86%	-0.21%	0.27%	0.77%	1.40%	2.04%	2.88%	4.45%
FHNRIV	-1.42%	-0.87%	-0.54%	-0.33%	-0.09%	0.01%	0.14%	0.43%	0.65%	0.99%	1.37%
MIX	-2.65%	-1.71%	-1.18%	-0.71%	-0.19%	0.23%	0.69%	1.33%	1.92%	2.63%	3.39%
MIXIV	-3.20%	-1.92%	-1.31%	-0.80%	-0.30%	0.02%	0.35%	0.86%	1.39%	2.10%	3.03%
MIXIVD	-3.16%	-1.84%	-1.31%	-0.80%	-0.30%	-0.01%	0.31%	0.80%	1.32%	1.95%	2.97%
Avg. across models	-3.00%	-1.76%	-1.20%	-0.70%	-0.18%	0.21%	0.62%	1.20%	1.77%	2.47%	3.57%
<i>Panel B. Using ARMA(1, 1) Intercepts and Residuals for Hedge Fund Returns</i>											
CAPM	-1.94%	-1.48%	-1.18%	-0.85%	-0.51%	-0.30%	-0.19%	-0.07%	0.01%	0.16%	0.43%
CAPMIV	-3.82%	-2.56%	-1.72%	-1.13%	-0.59%	-0.30%	-0.09%	0.22%	0.62%	1.02%	2.35%
CAPMIVD	-3.87%	-2.54%	-1.83%	-1.16%	-0.61%	-0.30%	-0.07%	0.24%	0.63%	1.07%	2.64%
FF	-1.99%	-1.54%	-1.23%	-0.99%	-0.64%	-0.39%	-0.20%	-0.03%	0.08%	0.26%	0.59%
FFIV	-4.13%	-2.76%	-1.98%	-1.43%	-0.73%	-0.25%	0.18%	0.76%	1.22%	1.94%	3.09%
FFIVD	-4.09%	-2.48%	-1.86%	-1.36%	-0.75%	-0.23%	0.21%	0.77%	1.38%	2.01%	3.51%
OPT	-3.18%	-2.08%	-1.61%	-1.16%	-0.69%	-0.34%	-0.05%	0.24%	0.51%	0.92%	1.69%
OPTIV	-3.95%	-2.64%	-1.81%	-1.25%	-0.64%	-0.26%	0.08%	0.61%	1.18%	1.91%	3.33%
OPTIVD	-4.29%	-2.65%	-1.87%	-1.31%	-0.75%	-0.29%	0.11%	0.63%	1.25%	2.26%	3.38%
FHNR	-3.79%	-2.48%	-1.67%	-1.18%	-0.64%	-0.13%	0.28%	0.82%	1.37%	2.01%	3.17%
FHNRIV	-1.66%	-0.95%	-0.64%	-0.41%	-0.13%	0.00%	0.09%	0.30%	0.53%	0.81%	1.31%
MIX	-3.27%	-2.23%	-1.70%	-1.31%	-0.80%	-0.44%	-0.13%	0.21%	0.48%	0.93%	1.47%
MIXIV	-3.48%	-2.15%	-1.59%	-1.08%	-0.50%	-0.13%	0.12%	0.51%	0.92%	1.49%	2.26%
MIXIVD	-3.69%	-2.10%	-1.58%	-1.02%	-0.48%	-0.13%	0.13%	0.53%	0.91%	1.43%	2.20%
Avg. across models	-3.37%	-2.19%	-1.59%	-1.12%	-0.60%	-0.25%	0.03%	0.41%	0.79%	1.30%	2.24%

models, roughly correspond to the alphas of the simulated funds with $\gamma \in (0, 0.1)$ and $\gamma \in (0.4, 0.5)$, respectively. Overall, these results show that the bottom half of the actual hedge funds cannot deliver abnormal performance, whereas the very top fund managers clearly have substantial skills.

Following Kosowski, Timmermann, Wermers, and White (2006) and Fama and French (2010), we consider an alternative way of comparing actual and simulated hedge fund returns. Panels A and B of Table 7 report the alphas of the after-fee returns adjusted for stale price bias using an ARMA(1, 1) model for the bottom and top 1%, 10%, 25%, and 50% of the 2,315 hedge funds at the 1:1 and 2:1 leverage ratios, respectively. Then, we report the percentage of the alphas of 1,000 simulated hedge funds at a given skill level, γ , that is higher than the actual alphas at those percentiles. If the percentage is 0%, then it means the actual performance is better than the simulated performance with a 100% empirical p -value. This comparison can be conducted for all the SDF models. To save space, we present results based only on MIX, given that MIX passes the specification test with reasonable pricing errors and might not overfit the data given its unscaled factors. Results using other models are qualitatively similar.

TABLE 7
Abnormal Returns of the Actual versus Simulated Long/Short Equity Hedge Funds

Table 7 compares the monthly abnormal returns (alphas) of the 2,315 actual long/short equity hedge funds with those of the simulated funds under the MIX model, which includes both the stock and option factors. Our sample contains monthly observations from Jan. 1996 to Dec. 2012. In the first two columns, we report the MIX alphas of the real funds at different percentiles. Then, we report the percentage of the simulated hedge funds at a given skill level, γ , that have higher alphas at those percentiles.

Percentiles for Actual Funds	MIX Alphas for Actual Funds	% of MIX Alphas from Simulated Returns That Are Higher Than the Actual Benchmark					
		$\gamma = 0$	$\gamma = 0.1$	$\gamma = 0.2$	$\gamma = 0.3$	$\gamma = 0.4$	$\gamma > 0.4$
<i>Panel A. Compare Actual ARMA(1, 1) Intercept and Residual Returns with Simulated After-Fee Returns, Leverage 1:1</i>							
1%	-3.27%	100%	100%	100%	100%	100%	100%
10%	-1.31%	100%	100%	100%	100%	100%	100%
25%	-0.80%	100%	100%	100%	100%	100%	100%
50%	-0.44%	100%	100%	100%	100%	100%	100%
75%	-0.13%	0%	100%	100%	100%	100%	100%
90%	0.21%	0%	100%	100%	100%	100%	100%
99%	1.47%	0%	0%	100%	100%	100%	100%
<i>Panel B. Compare Actual ARMA(1, 1) Intercept and Residual Returns with Simulated After-Fee Returns, Leverage 2:1</i>							
1%	-3.27%	100%	100%	100%	100%	100%	100%
10%	-1.31%	100%	100%	100%	100%	100%	100%
25%	-0.80%	100%	100%	100%	100%	100%	100%
50%	-0.44%	100%	100%	100%	100%	100%	100%
75%	-0.13%	0%	100%	100%	100%	100%	100%
90%	0.21%	0%	100%	100%	100%	100%	100%
99%	1.47%	0%	100%	100%	100%	100%	100%

In the first row in Panel A of Table 7, the alphas of the simulated returns at different skill levels are compared with those of the bottom 1% of the actual funds. We find that at any skill level, 100% of the simulated hedge funds have alphas higher than those of the bottom 1% of the actual funds, indicating that without any skill, all simulated hedge funds perform better than the bottom 1% of the actual funds. We find that 100% of the alphas of the simulated returns at $\gamma = 0$

are higher than those of the bottom 50% of t t funds, again suggesting that
t bottom 50% of t

Appendix. Scaled Signals

We define the signal as

$$(A-1) \quad s_{it} = \gamma \epsilon_{it} + (1 - \gamma) \sigma_i u_{it}.$$

We can compute the following (for later discussion, we drop all subscripts, i, t , for brevity):

$$(A-2) \quad E(s) = E[\gamma \epsilon + (1 - \gamma) \sigma u] = 0,$$

$$(A-3) \quad \text{var}(s) = \text{var}[\gamma \epsilon + (1 - \gamma) \sigma u] = [\gamma^2 + (1 - \gamma)^2] \sigma^2.$$

If we assume u and s are conditional normal, then we have

$$(A-4) \quad E(u|s) = E(u) + \frac{\text{cov}(u, s)}{\text{var}(s)} [s - E(s)] \\ = \frac{(1 - \gamma)s}{[\gamma^2 + (1 - \gamma)^2] \sigma},$$

$$(A-5) \quad \text{var}(u|s) = \text{var}(u) - \frac{\text{cov}^2(u, s)}{\text{var}(s)} \\ = 1 - \frac{(1 - \gamma)^2}{[\gamma^2 + (1 - \gamma)^2]} = \frac{\gamma^2}{[\gamma^2 + (1 - \gamma)^2]}.$$

Also from equation (A-1), the information ϵ can be computed as

$$(A-6) \quad \epsilon = \frac{1}{\gamma} [s - (1 - \gamma) \sigma u].$$

Now we can compute the conditional expectation of ϵ ,

$$(A-7) \quad E(\epsilon|s) = \frac{1}{\gamma} [s - (1 - \gamma) \sigma E(u|s)] \\ = \frac{1}{\gamma} [s - (1 - \gamma) \sigma \frac{(1 - \gamma)s}{[\gamma^2 + (1 - \gamma)^2] \sigma}] \\ = \frac{\gamma s}{[\gamma^2 + (1 - \gamma)^2]},$$

and the conditional variance of ϵ ,

$$(A-8) \quad \text{var}(\epsilon|s) = \text{var}\{1/\gamma [s - (1 - \gamma) \sigma u] | s\} \\ = \frac{(1 - \gamma)^2 \sigma^2}{\gamma^2} \text{var}(u|s) \\ = \frac{(1 - \gamma)^2 \sigma^2}{\gamma^2} \frac{\gamma^2}{[\gamma^2 + (1 - \gamma)^2]} \\ = \frac{(1 - \gamma)^2 \sigma^2}{[\gamma^2 + (1 - \gamma)^2]}.$$

Combining equations (A-7) and (A-8), we have

$$(A-9) \quad \frac{E(\epsilon_{it} | s_{it})}{\text{var}(\epsilon_{it} | s_{it})} = \frac{\frac{\gamma s_{it}}{[\gamma^2 + (1 - \gamma)^2]}}{\frac{(1 - \gamma)^2 \sigma_i^2}{[\gamma^2 + (1 - \gamma)^2]}} = \frac{\gamma}{(1 - \gamma)^2} \frac{s_{it}}{\sigma_i^2}.$$

Notice that for a given manager, the skill level, γ , is a constant. The function is well defined for any skill level between 0 and 1, including 0. When $\gamma = 1$, what the manager observes is the true signal without any noise, and the comparable measure should be $\epsilon_{it} / \sigma_i^2$.

References

- Agarwal, V., and N. Y. Naik. "Risks and Portfolio Decisions Involving Hedge Funds." *Review of Financial Studies*, 17 (2004), 63–98.
- Ahn, S. C., and C. Gadarowski. "Small Sample Properties of the GMM Specification Test Based on the Hansen–Jagannathan Distance." *Journal of Empirical Finance*, 11 (2004), 109–132.
- Ang, A.; R. J. Hodrick; Y. Xing; and X. Zhang. "The Cross Section of Volatility and Expected Returns." *Journal of Finance*, 61 (2006), 259–299.
- Bekaert, G., and R. Hodrick, *International Financial Management*, 2nd ed. Essex, UK: Pearson Education (2012).
- Ben Dor, A.; R. Jagannathan; and I. Meier. "Understanding Mutual Funds and Hedge Funds Styles Using Return-Based Analysis." *Journal of Investment Management*, 1 (2003), 97–137.
- Cao, C.; Y. Chen; B. Liang; and A. Lo. "Can Hedge Funds Time Market Liquidity?" *Journal of Financial Economics*, 109 (2013), 493–516.
- Chen, Y.; W. Ferson; and H. Peters. "Measuring the Timing Ability and Performance of Bond Mutual Funds." *Journal of Financial Economics*, 98 (2010), 72–89.
- Chordia, T.; R. Roll; and A. Subrahmanyam. "Recent Trends in Trading Activity and Market Quality." *Journal of Financial Economics*, 101 (2011), 243–263.
- Cochrane, J. *Asset Pricing*. Princeton, NJ: Princeton University Press (2005).
- Dybvig, P. H., and S. A. Ross. "Differential Information and Performance Measurement Using a Security Market Line." *Journal of Finance*, 40 (1985), 383–399.
- Fama, E., and K. French. "Common Risk Factors in the Returns on Stocks and Bonds." *Journal of Financial Economics*, 33 (1993), 3–56.
- Fama, E., and K. French. "Luck versus Skill in the Cross-Section of Mutual Fund Returns." *Journal of Finance*, 65 (2010), 1915–1947.
- Farnsworth, H.; W. Ferson; D. Jackson; and S. Todd. "Performance Evaluation with Stochastic Discount Factors." *Journal of Business*, 75 (2002), 473–583.
- Ferson, W., and S. R. Foerster. "Finite Sample Properties of the Generalized Methods of Moments Tests of Conditional Asset Pricing Models." *Journal of Financial Economics*, 36 (1994), 29–56.
- Ferson, W.; T. Henry; and D. Kisgen. "Evaluating Government Bond Fund Performance with Stochastic Discount Factors." *Review of Financial Studies*, 19 (2006), 423–455.
- Ferson, W.; S. Sarkissian; and T. Simin. "Asset Pricing Models with Conditional Alphas and Betas: The Effects of Data Snooping and Spurious Regression?" *Journal of Financial and Quantitative Analysis*, 43 (2008), 331–354.
- Fung, W., and D. A. Hsieh. "Empirical Characteristics of Dynamic Trading Strategies: The Case of Hedge Funds." *Review of Financial Studies*, 10 (1997), 275–302.
- Fung, W., and D. A. Hsieh. "The Risk in Hedge Fund Strategies: Theory and Evidence from Trend Followers." *Review of Financial Studies*, 14 (2001), 313–341.
- Fung, W.; D. A. Hsieh; N. Y. Naik; and T. Ramadorai. "Hedge Funds: Performance, Risk, and Capital Formation." *Journal of Finance*, 63 (2008), 1777–1803.
- Getmansky, M.; A. Lo; and I. Makarov. "An Econometric Analysis of Serial Correlation and Illiquidity in Hedge-Fund Returns." *Journal of Financial Economics*, 74 (2004), 529–609.
- Grinblatt, M., and S. Titman. "Portfolio Performance Evaluation: Old Issues and New Insights." *Review of Financial Studies*, 2 (1989), 393–421.
- Hansen, L. P., and R. Jagannathan. "Assessing Specification Errors in Stochastic Discount Factor Models." *Journal of Finance*, 52 (1997), 557–590.
- Jegadeesh, N., and S. Titman. "Returns to Buying Winners and Selling Losers: Implications for Stock Market Efficiency." *Journal of Finance*, 48 (1993), 65–91.
- Khandani, A., and A. Lo. "What Happened to the Quants in August 2007? Evidence from Factors and Transactions Data." *Journal of Financial Markets*, 14 (2011), 1–46.
- Kirby, C. "Measuring the Predictable Variation in Stock and Bond Returns." *Review of Financial Studies*, 10 (1997), 579–630.
- Kosowski, R.; A. Timmermann; R. Wermers; and H. White. "Can Mutual Fund 'Stars' Really Pick Stocks? New Evidence from a Bootstrap Analysis." *Journal of Finance*, 61 (2006), 2551–2595.
- Li, H.; Y. Xu; and X. Zhang. "Evaluating Asset Pricing Models Using the Second Hansen–Jagannathan Distance." *Journal of Financial Economics*, 62 (2010), 327–376.
- Merton, R. C. "On Market Timing and Investment Performance: An Equilibrium Theory of Values for Market Forecasts." *Journal of Business*, 54 (1981), 363–406.
- Mitchell, M., and T. Pulvino. "Characteristics of Risk and Return in Risk Arbitrage." *Journal of Finance*, 56 (2001), 2135–2175.
- Newey, W. K., and K. D. West. "A Simple, Positive Semi-Definite, Heteroskedasticity and Autocorrelation Consistent Covariance Matrix." *Econometrica*, 55 (1987), 703–708.

- Patton, A., and T. Ramadorai. "On the High-Frequency Dynamics of Hedge Fund Risk Exposures." *Journal of Finance*, 68 (2013), 597–635.
- Sharpe, W. F. "Capital Asset Prices: A Theory of Market Equilibrium under Conditions of Risk." *Journal of Finance*, 19 (1964), 425–442.
- Treynor, J. L., and K. Mazuy. "Can Mutual Funds Outguess the Market?" *Harvard Business Review*, 44 (1966), 131–136.